

Substituting the values of $\left(\frac{u}{U_\infty}\right)$ and η from eq's (5) and 7(a) into equation (i)

$$S^* = \sqrt{\frac{\nu x}{U_\infty}} \int_0^\infty (1-f') d\eta = \sqrt{\frac{\nu x}{U_\infty}} \lim_{\eta \rightarrow \infty} [\eta - f(\eta)]$$

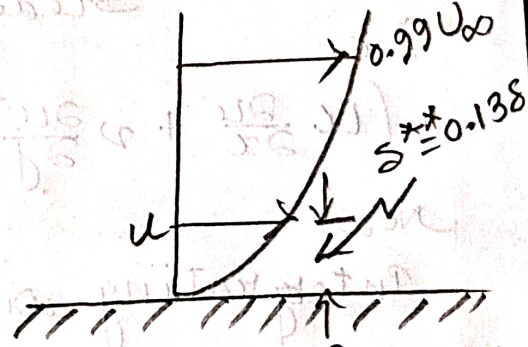
$$= 1.7208 \sqrt{\frac{\nu x}{U_\infty}} = \frac{1.7208x}{\sqrt{Re_x}} \rightarrow (ii)$$

* Momentum Thickness (S^{**}):-

It is defined as the loss of momentum in the boundary layer as compared with that of potential flow.

$$\int_0^\infty U_\infty^2 S^{**} = \int_0^\infty \rho u (U_\infty - u) dy$$

$$\Rightarrow S^{**} = \int_0^\infty \frac{u}{U_\infty} \left(1 - \frac{u}{U_\infty}\right) dy \rightarrow (iii)$$



Putting the value of $\frac{u}{U_\infty}$ and η from equations (5) & 7.(a)

$$S^{**} = \sqrt{\frac{\nu x}{U_\infty}} \int_0^\infty f'(1-f') d\eta$$

$$= 0.664 \sqrt{\frac{\nu x}{U_\infty}}$$

$$= \frac{0.664x}{\sqrt{Re_x}} \rightarrow (iv)$$

Values of the velocity profile shape

$$f'(\eta) = \frac{u}{U_\infty} = G \quad \text{and} \quad f''(\eta) = H$$

Table: The Blasius Velocity Profile $G = \frac{u}{U_\infty}$ and H

η	f	G	H
0	0	0	0.33206
0.2	0.00664	0.006641	0.33199
0.4	0.02656	0.13277	0.33147
0.8	0.10611	0.26471	0.32739
1.2	0.23795	0.39378	0.31659
1.6	0.42032	0.51676	0.29667
2.0	0.65003	0.62977	0.26675
2.4	0.92230	0.72899	0.22809
2.8	1.23099	0.81152	0.18401
3.2	1.56911	0.87609	0.13913
3.6	1.92954	0.92333	0.09809
4.0	2.30576	0.95552	0.06424
4.4	2.69238	0.97587	0.03897
4.8	3.08534	0.98779	0.02187
5.0	3.28329	0.99155	0.01591
8.8	7.07923	1.00000	0.00000