

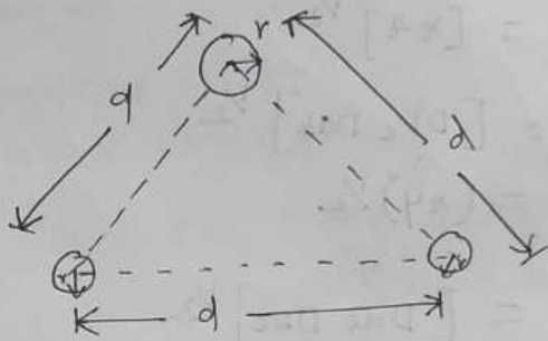
Three phase Transmission line

⇒ Three phase conductor configuration

- ① Symmetrical configuration
- ② Asymmetrical configuration.

Symmetrical configuration

- The three conductors are placed at the corners of an equilateral triangle.



a-phase mutual

$$D_{ma} = \left[\begin{matrix} D_{ab} & D_{ac} \end{matrix} \right]^{1/2} = D$$
$$D_{mb} = \left[\begin{matrix} D_{ab} & D_{bc} \end{matrix} \right]^{1/2} = D$$
$$D_{mc} = \left[\begin{matrix} D_{ac} & D_{bc} \end{matrix} \right]^{1/2} = D$$

GMR: $(GMR)_a = (GMR)_b = (GMR)_c$
 $= r'$

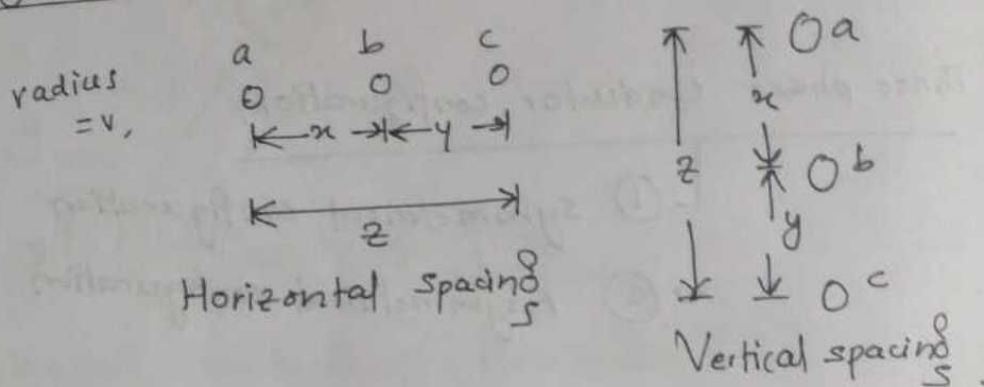
$$L_a = \frac{\mu_0}{2\pi} \ln \frac{GMD}{GMR}$$

$$= \frac{\mu_0}{2\pi} \ln \frac{D}{r'}$$

$$L_b = L_c = \frac{\mu_0}{2\pi} \ln \frac{D}{r'}$$

∴ Symmetrical $L_a = L_b = L_c$

Asymmetrical configuration



$$\therefore GMD = (GMD)_a = (Dm)_a$$

$$= [D_{ab} D_{ac}]^{1/2}$$

$$= [xz]^{1/2}$$

$$(Dm)_b = [D_{bc} D_{ab}]^{1/2}$$

$$= (xy)^{1/2}$$

$$(Dm)_c = [D_{ac} D_{bc}]^{1/2}$$

$$= (zy)^{1/2}$$

if radius ' r ' is same in all phase, then -

$$(GMR)_a = (GMR)_b = (GMR)_c = r'$$

Therefore, inductance,

$$L = \frac{\mu_0}{2\pi} \ln \frac{GMD}{GMR}$$

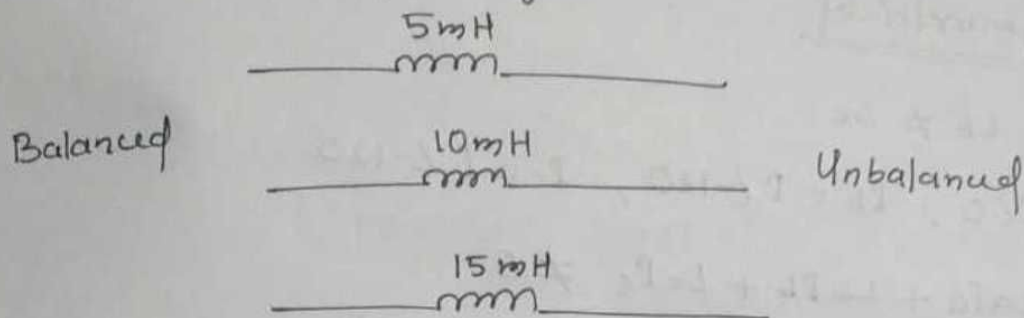
$$L_a = \frac{\mu_0}{2\pi} \ln \frac{D_{ma}}{r'}$$

$$L_b = \frac{\mu_0}{2\pi} \ln \frac{D_{mb}}{r'}$$

$$L_c = \frac{\mu_0}{2\pi} \ln \frac{D_{mc}}{r'}$$

Since, mutual GMD are unequal, their inductance are also unequal.

* consider balanced voltage.



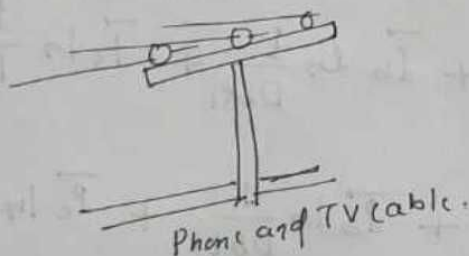
$$(\text{drop})_a \neq (\text{drop})_b \neq (\text{drop})_c$$

Asymmetrical \rightarrow Unbalanced receiving end voltages

Radio Interference

\Rightarrow The flux produced by power lines links the telephone conductors and induces an emf.

\Rightarrow The emf induced by power line in telephone line interferes with the signal carried by telephone conductors.



Faraday's law \Rightarrow emf.

Symmetrical and Asymmetrical

Symmetrical:

$$L_a = L_b = L_c$$

$$I_a = I/3$$

$$I_b = I/3$$

$$I_c = I/3$$

$$\Psi = LI$$

$$\Psi = L_a I_a + L_b I_b + L_c I_c$$

$$= L(I_a + I_b + I_c)$$

$$= 0, \text{ emf} = 0,$$

\Rightarrow so, symmetrical does not cause any disturbance.

Asymmetrical

$$L_a \neq L_b \neq L_c$$

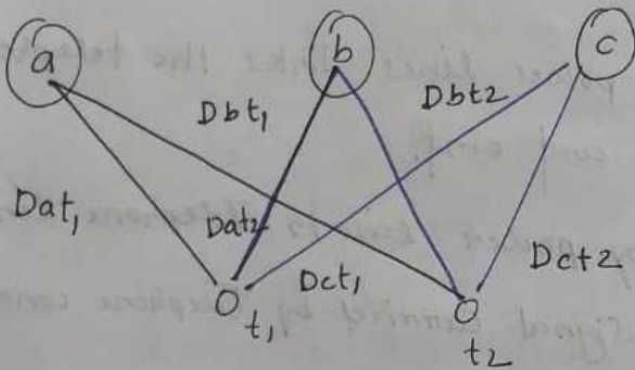
$$\angle a = \angle 0, \angle b = \angle -120, \angle c = \angle -120$$

$$\Psi = L_a \angle a + L_b \angle b + L_c \angle c \neq 0$$

$$e \neq 0$$

⇒ Radio interference in asymmetrical configuration.

EMF induced



$$\lambda = \frac{\omega_0}{2\pi} \sum_{j=1}^n I_j \ln \frac{1}{D_{ij}}$$

$$\lambda_{t1} = \frac{\omega_0}{2\pi} \left[\vec{I}_a \ln \frac{1}{D_{at1}} + \vec{I}_b \ln \frac{1}{D_{bt1}} + \vec{I}_c \ln \frac{1}{D_{ct1}} \right]$$

$$\lambda_{t2} = \frac{\omega_0}{2\pi} \left[\vec{I}_a \ln \frac{1}{D_{at2}} + \vec{I}_b \ln \frac{1}{D_{bt2}} + \vec{I}_c \ln \frac{1}{D_{ct2}} \right]$$

$$e = -\frac{d\lambda}{dt}, \quad e = -j\omega\lambda$$

⇒ '-j' emf lags λ by 90°

$$e_1 = -j\omega\lambda_{t1}, \quad e_2 = -j\omega\lambda_{t2}$$

$$e_{net} = e_1 - e_2$$

$$= -j\omega(\lambda_{t1} - \lambda_{t2})$$

$$\lambda = \lambda_{t1} - \lambda_{t2}$$

$$\lambda = \frac{\mu_0}{2\pi} \left[2a \ln \frac{D_{a2}}{D_{a1}} + 2b \ln \frac{D_{b2}}{D_{b1}} \right] \quad \because \log(a-b) = \ln\left(\frac{a-b}{1}\right)$$

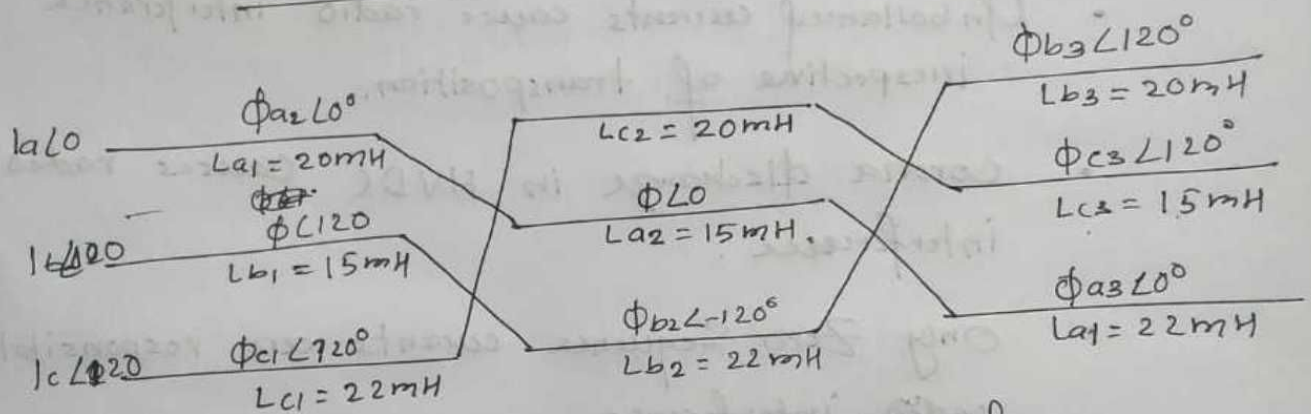
$\lambda =$ determined

$$M = \frac{\lambda}{I} \quad m = \text{mutual inductance}$$

$I =$ rms current carried by power line

$$E = \omega \lambda = \text{emf.}$$

Transposition



\Rightarrow change their position at regular interval.

$$L = f(GMD, GMR)$$

$$GMR = r'$$

$GMD =$ depends on conductor position.

GMD, GMR \downarrow radius, conductor position

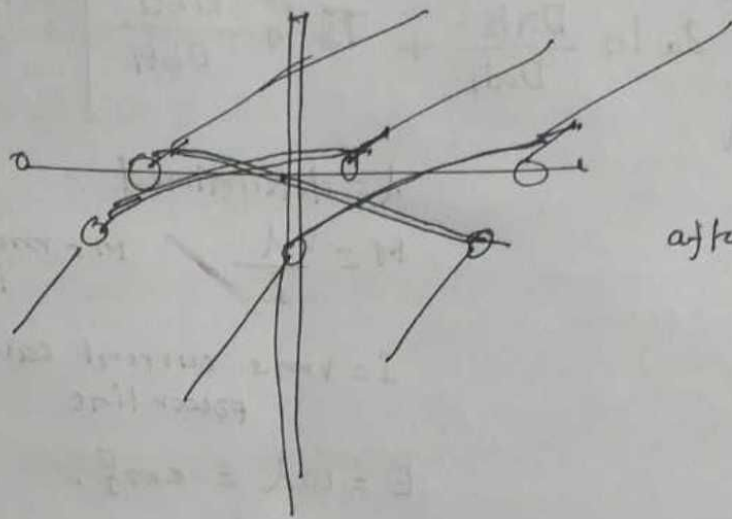
\Rightarrow inductance does not depend on the phase current it depends on position of the conductor.

$$\phi_a = 20\text{mH } I_a + 15\text{mH } I_a + 22\text{mH } I_a$$

$$L = 20\text{mH} + 15\text{mH} + 22\text{mH}$$

$$= 57\text{mH}$$

$$\boxed{L_b = L_c = L_a.}$$



after ICM.

Unbalanced currents

- Unbalanced currents cause radio interference irrespective of transposition.
- Corona discharge in HVDC causes radio interference.
- Only zero sequence currents are responsible for radio interference.